Application of ground-penetrating radar and high-density electrical sounding for the study of seasonally frozen ground

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Abstract

Ground-penetrating radar (GPR) and high-density electrical sounding surveys were conducted on a seasonally frozen ground at the Kitami Institute of Technology, northern Japan. The GPR survey detected the frozen ground as a weak echo zone in two and/or three dimensions. The high-density electrical sounding surveys showed that the electrode arrangement of the Wenner array effectively revealed the frozen layer as a resistive zone. The frost depth estimated from both surveys, especially the GPR profile, corresponded well to measurement done by a frost depth meter (frost tube). The results of this study show the applicability of non-destructive surveys in geophysical exploration on seasonally frozen ground. GPR surveys could be especially effective in conducting repeated investigation on large areas of seasonally frozen ground.

1. Introduction

Formation of frozen ground causes frost heave. In cold regions, this frost heave may disrupt human lives due to the deterioration of pavements and/or buildings. The mechanism of frozen ground development has been studied to date. In general, a frost depth meter (frost tube) and thermometer are used to investigate the distribution and thickness of the seasonally frozen ground. These apparatus are inserted vertically into the target spot; therefore, the depth information is limited to that spot. In recent years, a number of geophysical explorations have been conducted to study frozen ground (e.g., Hauck, 2005; Yoshikawa et al., 2006), and further development of these techniques is anticipated in the future. Resistivity prospecting is one of the major methods used to estimate frost depth or frozen areas (e.g., Ishikawa and Hirakawa, 2000; Hauck et al., 2003). However, these studies were conducted in permafrost areas, and few studies have been conducted on seasonally frozen ground (e.g., Takami et al., 2002). In this study, we applied a ground penetrating radar (GPR) survey and high-density electrical sounding (resistivity sounding) to estimate the frost depth of seasonally frozen ground at experimental sites in the Kitami Institute of Technology, northern Japan.

2. Outline of experiments

GPR survey is a visualization technique used to obtain an image of subsurface structure by the reflection, permeation, and refraction of radio waves at subsurface electromagnetic boundaries. It has also been used to study the subsurface permafrost distribution (e.g., Hinkel et al., 2001). On the other hand, high-density electrical sounding represents resistivity prospecting using several electrodes arranged in a straight line. We examined the efficiency of each method in detecting seasonally frozen ground by comparing the results obtained from them.

We surveyed two sites (A and B) at the Kitami Institute of Technology in February 2000. The apparatus used for the GPR survey was a pulse EKKO 1000 (Sensors & Software Inc., Canada). The two antennas (receiver and transmitter) were fixed to maintain an antenna separation of 0.25 m for 450-MHz and 0.17 m for 900-MHz. These antennas were moved systematically along the survey line with a spacing of 0.1 m. The profile analysis was performed using dewow filter (signal saturation correction, which removes an unwanted low frequency) and filter of vertical and horizontal direction.

The apparatus used for the high-density electrical sounding was E60B (GeoPen, China). The Wenner electrode configuration (Telford et al., 1990) was adopted because it provides an excellent estimation of a
horizontal structure. We performed two-dimensional model analysis by applying inversion (least-squares method) to the primary model using the software E-Tomo (Dia Consultants Co., Japan).

2.1 Survey at Site A

Site A is a rectangular area (5 m × 2 m) composed of volcanic ash clay from the ground surface to a depth of approximately 1 m with basal ash lying below this depth. Frost tubes, thermometers and a device to observe the amounts of frost heaving are also installed at this site (Fig. 1). The frost tube consists of inner and outer tubes. The inner tube, which is made of acrylic resin and filled with 1% methylene blue aqua, has an outer caliber of 25 mm, inner caliber of 20 mm, and length of 1.5 m. The outer tube, made of vinyl chloride, has outer and inner calibers of 38 and 30 mm, respectively. The frost depth was observed daily and the ground temperature was measured every two hours from November to March. The temperatures were measured at vertical spacing of every 5 cm (0–1 m in depth) and every 10 cm (1–1.2 m in depth). In addition, the snow accumulated on the surface of the investigated area was removed during winter.

We set 21 survey lines at Site A. Line 1 (5.1 m in length, survey point spacing of 0.1 m) was set parallel to the longitudinal direction of this area, and both surveys were conducted along this line. Lines 2–21 (1.5 m in length, survey point spacing of 0.1 m and survey line spacing of 0.2 m) were set up perpendicular to Line 1, and only the GPR survey was performed along these lines (Fig. 2).

In the GPR survey, an antenna with a center frequency of 450-MHz was primarily used, while surveys using a 900-MHz antenna were also conducted on Lines 1, 2, 7, 16, and 18. Radio waves radiate conically from the antenna into the ground. If the average relative dielectric constant of frozen ground is assumed to be 6 (Society of Exploration Geophysicists, 1998), the effective distance is approximately 0.2 m at the depth of 0.5 m from a survey point in the direction perpendicular to the scanning antenna direction using the 450-MHz antenna. Thus, the surveys cover all the target area with these survey points and lines spacing. The spatial resolutions of the radio waves in the ground are approximately 0.1 m at 450-MHz and 0.06 m at 900-MHz, as estimated from the propagation velocity of the radio waves (0.10–0.12 m ns⁻¹ described in subsection 2.3). Thus, these resolutions are sufficient to estimate the distribution of the frozen ground.

High-density electrical sounding was conducted along Line 1. The electrode spacing and length of survey line were set to 0.2 and 5.2 m, respectively. Since pitching electrodes into the frozen ground was difficult, it was expected that the ground resistance would increase.

2.2 Survey at Site B

Site B is an artificial pit area with a depth of 1.3 m; it is surrounded by a concrete wall and filled with testing soil (Fig. 3). The internal testing soil is composed of volcanic ash clay (0–0.9 m in depth) and gravel (0.9–1.3 m in depth) (Fig. 4). A water pipe is installed at the bottom of the pit, where the gravel is filled to control a uniform groundwater level. As shown in Fig. 4, we set 14 survey lines (2.7 m in length, survey point spacing of 0.1 m, and survey line spacing of 0.2 m) for the GPR survey. A 450-MHz antenna was used at this site.

2.3 Estimation of propagation velocity of radio waves

In the GPR survey, we did not conduct the com-
mon midpoint (CMP) survey (Telford et al., 1990),
which estimates the propagation velocity of radio
waves in the ground. Consequently, at each site, the
propagation velocity is estimated as follows:

[1] Site A: The propagation velocity of the radio
waves is calculated using the following equation:

\[ V = \frac{c}{\sqrt{\varepsilon_r}} \]

where \( c \) is \( 3.0 \times 10^8 \text{ m s}^{-1} \) and \( \varepsilon_r \) is the relative
dielectric constant of the medium. When the relative
dielectric constant of the frozen ground is 4–8 (Society
of Exploration Geophysicists, 1998), the propagation
velocities become 0.11–0.15 m ns\(^{-1}\). Because the rela-
tive dielectric constant of frozen ground is affected by
the amount of ice and unfrozen water in the soil, the
velocities at this site could not be ascertained. There-
fore, we used the central value of 0.12 m ns\(^{-1}\) (\( \varepsilon_r = 6 \)) to
calculate the approximate depth.

[2] Site B: The strongest reflection appeared at
25 ns in travel time, which was the reflection from the
basal concrete wall at the depth of 1.3 m. Subse-
quently, the velocity was calculated to be 0.10 m ns\(^{-1}\),
which we considered to be the average propagation
velocity in this pit.

3. Results

3.1 Site A

Table 1 shows the daily mean temperature on the
surveyed day. Figure 5 shows the water content
measured from a boring core sample at Site A. The
frost depth measured using the frost tube was 76.1 cm.
As the amount of frost heaving was 6.2 cm, the thick-
ness of the frozen ground was approximately 82 cm.

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Fig. 3. Photograph of Site B.

Fig. 4. Structure of the artificial pit at Site B. [A] A
vertical cross section. [B] A horizontal layout
from the top. Thick arrows are the survey lines.
Fig. 5. The water content measured from a boring core at Site A.

Figure 6 shows the GPR profile along Line 1 obtained using the center frequency of the 900- and 450-MHz GPR antennas. The color tones of the profile represent the strength of the echo; the darker color indicates a stronger echo. The differing resolutions at the two frequencies resulted in slightly different distributions of echo strength at the different depths. However, the overall echo patterns were almost similar to each other. A weak echo zone above the depth of about 0.6–0.8 m corresponds to the frozen ground, as can be seen on comparison with the abovementioned measurements. Thus, a strong echo zone below this depth represents unfrozen ground.

Figure 7 shows the survey profiles of three typical survey lines (Lines 9, 11, and 18) obtained using the center frequency of the 450-MHz GPR antennas. The weak echo zone between the surface and the depth of 1 m is recognized to be frozen ground (as in the case of Line 1), and the freezing front is found to be uneven. This indicates that the depth of the freezing front or the thickness of the frozen ground varies in each survey line. A lengthwise echo in the deeper part around the centers of Lines 9 and 11 may be a reflection from the buried thermometer.

Thus, the results of the GPR profiles correspond well with the actual frost depth, and the three-dimensional figure (Fig. 8) composited from the profiles along Lines 2–21 shows similar result. This shows the unevenness of the freezing front in a small area. In addition, the depth of the freezing front is deeper around the center of the survey area. It appears that the ground does not freeze easily near the edge of the survey area, due to the warming effects of the snow cover on the neighboring areas.

At this site, a high-density electrical resistivity survey was conducted along Line 1 using the Wenner array (Fig. 9). In Fig. 9, the upper and lower figures show a typical figure of electrode arrangement and the theoretical distribution of the measurement points, respectively. Figure 10 shows the interpreted result. There exists a resistive layer above the depth of approximately 1 m, except for the subsurface. Considering the results of Table 1, it is presumed that the resistive layer at the depth of 1 m corresponds to the frozen ground.

3.2 Site B

In this site, the frost depth measured using the frost tube was 57.5 cm, and the amount of frost heaving was 12.9 cm, indicating that the thickness of the frozen ground was about 70 cm. The GPR profiles of Lines 7 and 12 measured using a 450-MHz antenna are shown in Fig. 11. A strong echo at the travel time (left axis) of 25 ns was considered to be from the concrete bottom of the pit at the depth of 1.3 m, while a weak echo zone was observed from the surface to a depth of approximately 0.6 m. We considered the weak echo zone to be the frozen ground, although the freezing depth estimated from the GPR survey differed slightly from that measured using the frost tube. We inferred that this difference was caused by the application of the average propagation velocity of the radio wave to the profile analysis. The irregular echo around 0.5–1 m in the horizontal direction on Line 12 could be attributed to the influence of the frost heaving block (an observation device).

There is a strong echo from the freezing front to a depth of approximately 0.9 m, corresponding to the unfrozen volcanic ash clay layer. The lower weak echo zone corresponds to the gravel layer. This indicates that the relative dielectric constant of the gravel layer is higher than that of the volcanic ash clay layer. In general, the relative dielectric constant of volcanic ash clay and gravel are in the range of 2 to 6 when they are dry (Society of Exploration Geophysicists, 1998; Kobayashi and Sato, 2004). However, the echo pattern of the GPR survey indicates obvious differences in their dielectric properties. This was interpreted as an indication that the gravel layer contained many air gaps filled with unfrozen water and that it had a higher relative dielectric constant.

Figure 12 shows the three-dimensional figures composited from the profiles along all survey lines; in this figure, [A] shows the overview and [B] and [C] show the partial cross sections of [A] at arbitrary
Fig. 6. GPR profiles (each upper figure) and the interpreted results (each lower figure) along Line 1 at Site A. The left axis shows the travel time, and the right axis shows the estimated depth. [A] The center frequency of 900-MHz. [B] The center frequency of 450-MHz.
Fig. 7. GPR profiles (upper figures) and interpreted results (lower figures) along Line 9, 11, and 18 at Site A using the center frequency of 450-MHz GPR antennas.

Fig. 8. The three-dimensional figure composited from the profiles along Lines 2-21 at Site A.

Fig. 9. A typical figure of electrode arrangement (upper figure) and the theoretical distribution of the measured points (lower figure) at the Wenner array. The C and P show an electric current and electric potential electrodes, respectively. The “a” shows electrode spacing or survey depth.
4. Discussions

The frozen ground was detected as a weak echo zone in the GPR profile. This weak echo zone may have appeared because the relative dielectric constant was homogenized due to the growth of the frozen ground and an increase in the amount of ice.

In the case of Site A, the freezing front detected on the GPR profiles is uneven in a small area. In other words, the frost depth measured using the frost tube does not represent the typical frost depth around the investigation area, unless the measurement is performed at a large number of well-distributed points.
seasonally frozen ground. Moreover, in the resistivity survey, there exists the possibility of increase in the ground resistance and decrease in the electric potential due to the water from melting snow. Therefore, we consider that the GPR survey is more suitable for investigating the distribution of seasonally frozen ground over a large area.

At Site B, the freezing front presumed from the profile is flat, in contrast to Site A. The GPR echo pattern of all survey lines are similar, which may be caused by the artificially controlled water supply in the pit and the uniform rate of ground freezing.

5. Conclusions

The efficiency of non-destructive investigations on frozen ground was studied through experimental surveys. A GPR survey and a high-density electrical sounding method revealed the following results:

1. In the GPR study, seasonally frozen ground was detected as a weak echo zone. We considered that the radio waves were not strongly reflected because an increase in the amount of ice in the seasonally frozen ground had homogenized the relative dielectric constant.

2. From the GPR profiles, the freezing front could be displayed as a planar structure. At Site A, the detected freezing front was uneven. The thickness of the seasonally frozen ground may change depending on the location, even in a small area under natural conditions. Therefore, expansive investigation and three-dimensional analysis using a GPR survey are important and effective methods for the study of seasonally frozen ground distribution.

3. In an artificial pit (Site B), where the soil was packed into the pit and the water supply was controlled, the freezing front was ascertained to be almost flat based on the GPR profiles.

4. The electrical resistivity survey using the Wenner array detected the seasonally frozen ground as a resistive layer. The area corresponded well to the seasonally frozen ground area measured by the frost tube.

The GPR survey and high-density electrical sounding are both effective methods for the study of seasonally frozen ground. A comparison of the two methods reveals that the GPR survey offers higher mobility and repeatability, and can detect the planar structure of the freezing front more clearly. Further, in the resistivity survey, there exists a possibility that the ground resistance may increase and the electric potential may decrease due to the water from melting snow. Therefore, the GPR survey is more suitable for investigating the distribution of seasonally frozen ground over a large area, and it will contribute to the study of frozen ground formation by continuous observation of the same area.
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References


